

## Quantum Physics PHY4215 - Exercise Sheet 3

1. The power transmitted through an area  $A$  perpendicular to a plane wave is given by

$$P = \frac{1}{\mu_0 c} E_0^2 A \sin^2(kz - \omega t)$$

as described, for example, in Krane eq. 3.8. The time-averaged power (Krane eq. 3.10) is given by

$$\frac{P}{A} = \frac{1}{2\mu_0 c} E_0^2$$

First fix  $z = 0$  and do the time averaging. Then explain the time averaging for general  $z$ . In both cases, consider an integration over one time period  $T = \frac{2\pi}{\omega}$ . [10]

*Hint : In doing the time averaging, you will find it useful to note that  $\cos 2\theta = 1 - 2\sin^2 \theta$ .*

2. Find the momentum of

- (a) a 10.0 MeV gamma ray.
- (b) a 25-keV X ray.
- (c) a 1.0-  $\mu\text{m}$  infra-red photon.
- (d) a 150-Mhz radio-wave photon.

Express the momentum in  $\text{kg m/s}$  and  $\text{eV}/c$ .

[8]

3. Electrons are emitted when an ultraviolet light source of wavelength  $\lambda$  illuminates a certain metal surface. If you wanted to increase the number of electrons per unit time emitted from the surface, which one or more of the following measures would work ?

- (a) increase the frequency of the light source.
- (b) increase the wavelength of the light source.
- (c) add a second light source identical to the first light source.

[6]

4. When photons of wavelength 477 nm are incident on a metal surface, electrons of maximum kinetic energy 1.41 eV are emitted from the surface. What is the minimum energy needed to remove an electron from this metal ?

[8]